

$$x^n dx = x^{n+1} / (n+1) + c$$

$$\int a^x dx = ax^{1/a} + c$$

TEXTBOOK

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I.A. Narkyevich

MATHEMATICS



«GEOTAR-Media»
PUBLISHING GROUP

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